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Printed Pages – 5 TCS – 301

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID: 1064 Roll No.

B.Tech.

THIRD SEMESTER EXAMINATION, 2006-07

Total Marks: 100

DISCRETE STRUCTURE

Time : 3 Hours

4.7

- (i) Attempt ALL questions.
- (ii) All questions carry equal marks.
- (iii) Be precise in your answer.
- 1. Attempt any four parts of the following: (5x4=20)
 - (a) (i) Show that for any two sets A and B $A (A \cap B) = A B$.
 - (ii) Give the power set of the set given below :
 - $A = \{a, \{b\}\}$
 - (b) (i) Let R be a binary relation defined as $R = \{ \langle a, b \rangle \in \mathbb{R}^2 \mid a b \leq 3 \}$ determine whether R is reflexive, symmetric, anti symmetric and transitive.
 - (ii) How many distinct binary relations are there on the finite set A?
 - (c) Let $X = \{1, 2, ..., 7\}$ and $R = \{\langle x, y \rangle | x y \text{ is divisible by 3}\}$ show that R is an equivalence relation.

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Note:

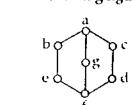
|Turn Over

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- Define a group. Let $S = \{0, 1, 2, 3, 4, 5, 6, 7\}$ (c) and * denote "multiplication modulo 8 i.e. $x*y = (xy) \mod 8$.
 - Write three distinct groups (G, *) where $G \subseteq S$ and G has two elements.
- (d) What do you mean by group homomorphism and group isomorphism? Explain with example.
 - If (R, +, •) is a ring with unity, then show that, (e) for all ack.
 - (-1).a = -a(i) (ii) $(-1) \cdot (-1) = 1$
- **(f)** Find the elements and the multiplication table of the symmetric groups S₃.
- 3. Attempt any four parts of the following: (5x4=20)(a) Define Poset. Give an example of a set X such

that $(P(x), \subseteq)$ is a totally ordered set.

- (b) Let A be a given finite set and P (A) its power set. Let \subseteq be the inclusion relation on the elements of P (A). Draw the Hasse diagrams of $(P(A), \subseteq)$ for
 - (c) In the lattice defined by the Hasse given by the following figure:



 $A = \{a, b, c\}.$

How many complements does the elements 'e' have? Give all.

(d) List all possible functions from X={a, b, c} to
 y={0, 1} and indicate in each case whether the

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function is one to one, is onto and is one to one onto.

(i) Define an equivalence class generated by the elements of a set on a given equivalence

(ii) Let F_x be the set of all one to one onto mapping from X onto X, where $X = \{1, 2, 3\}$. Find all the elements of F_x and find the inverse of each element.

(f) State and prove Pigeon hole principle.

relation.

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(e)

2. Attempt any four parts of the following: (5x4=20)(a) Let (A, *) be a semigroup, further more for every

(i) Show that for every a in A

a and b in A, if $a \neq b$, then $a*b \neq b*a$.

a*a = aShow that for every a, b in A

(iii) Show that for every a, b, c in A a*b*c = a*c

(b) Let G_1 and G_2 be sub group of a group G.

Is $G_1 \cup G_2$ always a subgroup of G?

ways a saugroup of G

Show that $G_1 \cap G_2$ is also a subgroup of G.

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(i)

(ii)

(ii)

a*b*a = a

(d) Define a boolean function. For any x and y in a boolean algebra show that x v y = x ∧ y.
(e) Write the following Boolean expressions in an equivalent product of sums canonical form in three variables x₁, x₂ and x₃.
(i) x₁*x₂
(ii) x₁ ⊕ x₂

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(ii) Binary tree (iii) Binary search tree

Define following terms:

Rooted tree

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(f)

(i)

- 4. Attempt any two parts of the following: (10x2=20)(a) (i) What is difference between conditional and biconditional statements? Explain with
- example.

 (ii) Make a truth table for: $(P \rightarrow Q) \land (P \rightarrow R)$.
 - (b) Show that the truth values of the following formulas are independent of their components.
 - (i) $(P \land (P \rightarrow O)) \rightarrow O$
 - (ii) (P→Q)⊋a(HP∨Q)
 - (ii) $(P \rightarrow Q) \oplus \tau (P \vee Q)$ (iii) $(P \rightarrow Q) \wedge (Q \rightarrow R) \mapsto (P \rightarrow R)$
- (c) Show that given formula is a tautology

 $((P \lor Q) \land T(TP \land (TQ \lor TR))) \lor (TP \land TQ) \lor (TP \land TR) \rightarrow$

- 5.
 - Attempt any two parts of the following:
 - (a) Solve the following recurrence relations:
 - $a_{n+1} 1.5 \ a_n = 0, \ n \ge 0$ (i)
 - $a_n = 5a_{n-1} + 6a_{n-2}$, $n \ge 2$, $a_0 = a_1 = 3$ (ii)

of the graph with example.

- (b) Describe the 1-isomorphism and 2-isomorphism
- Write short notes on any two of the following: (c)
- (i) Complete bipartite graph
 - (ii) Hamiltonian paths and circuit
 - Chromatic number of a graph (iii)
 - (iv)
 - Eular graphs