Roll No. $\square$

MCA
(SEM. II) THEORY EXAMINATION 2017-18
COMPUTER BASED NUMERICAL AND STATISTICAL TECHNIQUES
Time: 3 Hours
Note: Attempt all Sections. If require any missing data; then choose suitably.

## SECTION A

1. Attempt all questions in brief.
a. Prove that $\mu \delta=\frac{1}{2} \Delta E^{-1}+\frac{1}{2} \Delta$
b. Write down Newton's Backward Interpolation Formula.
c. Suppose .333 is used as an approximation to $\frac{1}{3}$. Find the absolute and relative errors.
d. Explain the Simpson's rule.
e. Write short notes on Regression Analysis.
f. What do you mean by forecasting.
g. Write components of time-series.

## SECTION B

2. Attempt any three of the following:
a. Find a real root of $x^{3}-x-1=0$ between 1 and 2 by bisection method. Compute five iterations.
b. Apply Gauss's forward formula to find the value of $u 9$, if $u_{0}=14, u_{4}=24$, $\mathrm{u}_{8}=32, \mathrm{u}_{12}=35, \mathrm{u}_{16}=40$
c. Using Newton's divided differences formula, evaluate $f(9)$ for

| x | 5 | 7 | 11 | 13 | 17 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{f}(\mathrm{x})$ | 150 | 392 | 1452 | 2366 | 5202 |

d. Solve the equations by Gauss-Seidal method
$20 \mathrm{x}+\mathrm{y}-2 \mathrm{z}=17$
$3 x+20 y-z=-18$
$2 x-3 y+20 z=25$
e. The table given below reveals the velocity ' $v$ ' of a body during the time ' $t$ ' specified. Find its acceleration at $t=1.1$

| $t$ | 1.0 | 1.1 | 1.2 | 1.3 | 1.4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $v$ | 43.1 | 47.7 | 52.1 | 56.4 | 60.8 |

SECTION C
3. Attempt any one part of the following:
$7 \times 1=7$
(a) Write the algorithm of Bisection and Regula-falsi method. Also explain what is the difference between them.
(b) Using Newton-raphson method, find the real root of the equation $3 x=\cos x+1$ correct to four decimal places.
4. Attempt any one part of the following:
(a) What do you mean by Interpolation and Derive the Newton's Forward Interpolation Formula.
(b) Use Gauss's Backward formula to find the population for the year 1936 given

| Year | 1901 | 1911 | 1921 | 1931 | 1941 | 1951 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Population <br> (in thousand) | 12 | 15 | 20 | 27 | 39 | 52 |

5. Attempt any one part of the following:
(a) Find $\int_{\mathbf{0}}^{\mathbf{0}} \frac{e^{x}}{1+x} d x$ approximately using simpson's $3 / 8^{\text {th }}$ rule on integration.
(b) Solve the equation $\frac{d y}{d x}=\boldsymbol{x}+\boldsymbol{y}$ with initial condition $\mathrm{y}(0)=1$ by Runge-Kutta rule, from $\mathrm{x}=0$ to $\mathrm{x}=0.4$ with $\mathrm{h}=0.1$.
6. Attempt any one part of the following:
(a) Solve $\frac{d y}{d x}=\mathbf{1}+\boldsymbol{x} \boldsymbol{y}$ with $\mathrm{x}_{0}=2, \mathrm{y}_{0}=0$ using Picard's method of successive approximations.
(b) Obtain a relation of the form $\boldsymbol{y}=\boldsymbol{a} \boldsymbol{e}^{\boldsymbol{b} \boldsymbol{x}}$ for the following data by the method of least squares:

| x | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 1.6 | 4.5 | 13.8 | 40.2 | 125 | 300 |

7. Attempt any one part of the following:
(a) Define Chi-square test and discuss the various application of its in data analysis.
(b) Describe Moving average method. From the following data, calculate 4 years moving average

| Year | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Output | 20 | 21 | 23 | 22 | 25 | 24 | 27 | 26 | 28 | 30 |

