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(Following Paper II) and	d Roll No. to	be filled	in you	r Ans	wer I	Joek)
PARR ID: 9610	Roll No.					\prod

B. Tech. (Second Semester) Theory

Examination, 2010-11

11- 16- 12 WE ___

MATHEMATICS-II

Time: 3 Hours] [Total Marks: 100

Note: Attempt the questions from each Section as indicated. The symbols have their usual meaning.

Section-A

Attempt all questions of this Section. Each question carries equal marks. 2×10=20

1. (i) In the RC-circuit where C=0.01 F; R=20 ohms, $E_0=10$ V. The current I(t), assuming that capacitor is completely uncharged, is

given as I(t) =_____

(ii) The differential equation for which $xy = ae^{x} + be^{-x} + x^{2}$ is the solution, is given

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(iii) If
$$\frac{d}{dr}(J_0) = nJ_1$$
, then value of n is _____.

$$2x^2y'' + xy' + (x^2 - 3)y = 0$$
 are

(v) The value of Inverse Laplace Transform
$$E^{-1}\left\{\frac{1}{\sqrt{3/2}}\right\}$$
 is given as:

(a)
$$\sqrt{\frac{t}{\pi}}$$

(b)
$$2\sqrt{\frac{t}{\pi}}$$

(c)
$$t^{3/2}$$

(d)
$$\sqrt{t}$$
.

then
$$L(e^{-t}f(3t))$$
 is:

(a)
$$\frac{e^{-1/(\xi+1)}}{(z+1)}$$

(b)
$$\frac{e^{-3/(s+1)}}{(s+1)}$$

If Laplace Transform of $L\{f(t)\} = \frac{e^{-1/s}}{s}$,

(viii) The partial differential equation $\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial y^2} = \frac{1}{a^2} \frac{\partial u}{\partial t}$

$$\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial y^2} = \frac{1}{c^2} \frac{\partial u}{\partial t}$$

Elliptic Parabolic

(d) None of these. (3)

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- (ix) Match the following:
 - (a) One-dimensional (p) $\frac{\partial^2 u}{\partial x^2} = \frac{1}{h} \frac{\partial u}{\partial t}$ heat equation
 - (b) One-dimensional (q) $\frac{\partial^2 u}{\partial x^2} = -\frac{\partial^2 u}{\partial y^2}$ wave equation
 - (c) Two-dimensional (r) $\frac{\partial^2 u}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2}$ Laplace equation
 - (d) Two-dimensional (s) $\frac{\partial^2 u}{\partial x^2} = \frac{1}{c^2} \frac{\partial u}{\partial t} \frac{\partial^2 u}{\partial y^2}$ heat equation
- (x) The general solution of partial differential equation $p-q = \log(x+y)$ is given as _____.

Section-B

Attempt any three parts of the following, 10×3=30

- 2. (a) Find the complete solution of the differential equation $(D-2)^3 y = 17 e^{2x}$, where symbols have their usual meanings.
 - (b) Using power series method, obtain the solution for $x^2y^4 + x(x-1)y' + (1-x)y = 0$, about x=0.

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(4)

differential equation
$$y''+2y'+5y=e^{-t}\sin t$$
, $y(0)=0$, $y'(0)=1$.

(d) Obtain the Fourier series expansion of $f(x) = \left(\frac{\pi - x}{2}\right) \text{ in } 0 < x < 2$

$$\sin\left(\frac{\pi x}{2}\right) + 3\sin\left(\frac{5x\pi}{2}\right).$$
Section-C

- Attempt any two parts of the following:
 - Solve by method of variation of parameter (a) $(D^2-1)y = 2(1-e^{-2x})^{-1/2}$

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(b) Solve the system of simultaneous differential equations:

$$\frac{dx}{dt} + x - 2y = 0$$
, $\frac{dy}{dt} + x + 4y = 0$, $x(0) = y(0) = 1$.

- (c) Find the steady state solution in RLC circuit equation consisting of inductance L=0.05 H, resistance R=05 ohms and a condensor of capacitance 4×10⁻⁴ farad, if Q=I=0 when t=0 and there is an alternating emf of 200 cos 100 t. Find Q(t) and I(t).
- 4. Attempt any two of the following:
 - (a) Express the polynomial $f(x) = 4x^3 2x^2 3x + 8$ in terms of Legendre polynomials.
 - (b) Show that:

$$J_1''(x) = -J_1(x) + \frac{1}{x}J_2(x)$$
.

(c) Evaluate:

$$\int x^2 J_1(x) dx .$$

Attempt any two of the following:

of i
$$\frac{16}{(s-2)(s+2)^2}$$

$$f(t) = \begin{cases} \sin \omega t, & 0 < t < \frac{\pi}{\omega} \\ 0, & \frac{\pi}{\omega} < t < \frac{2\pi}{\omega} \end{cases}.$$

$$\int_{t=0}^{\infty} \int_{u=0}^{t} \frac{e^{-t} \sin u}{u} du dt = \frac{\pi}{4}$$

$$f(x) = x - x^2 \cdot \ln |0 < x < 1|.$$

(b) Find the Fourier series of :

$$f(x) = \begin{cases} 0 & \text{, when } -\pi \le x \le 0 \\ x^2 & \text{when } 0 \le x \le \pi \end{cases}$$

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(c) Find the general solution of partial differential equation:

$$(y^2 + z^2) p - xyq + zx = 0.$$

- Attempt any one of the following:
 - (a) In a telephone of wire of length l, a steady voltage distribution of 20 volts at the source end and 12 volts at the terminal end is maintained. At time t=0, the terminal is grounded. Assuming L=0, G=0, determine the voltage and current where symbols have their usual meanings.
 - (b) The temperature distribution in a bar of length π which is perfectly insulated at ends x=0 and $x=\pi$, governed by the partial differential equation $\frac{\partial u}{\partial t} = k^2 \frac{\partial^2 u}{\partial x^2}$. Assuming the initial temperature as $u(x,0) = f(x) = \cos x$, find the temperature distribution at any instant of time, k and ϵ being constants.