Printed Pages: 1 Roll No.										NCS062
---------------------------	--	--	--	--	--	--	--	--	--	--------

B.TECH. THEORY EXAMINATION (SEM–VI) 2016-17 COMPLEXITY THEORY

Time: 3 Hours Max. Marks: 100

Note: Be precise in your answer. In case of numerical problem assume data wherever not provided.

SECTION-A

1 Explain the following:

 $(10 \times 2 = 20)$

- a) Turning Machine
- **b)** Parallel computation
- c) Diagonalisation
- **d**) Uncomputable function
- e) NP-Complete problem
- **f**) Counting problems
- **g**) Interactive proof
- **h**) Approximability and inapproximability
- i) Adleman's theorem
- j) Fooling set

SECTION-B

2 Attempt any five of the following:

 $(10 \times 5 = 50)$

- a) What do you mean by complexity classes? Discuss the relationship among the complexity classes.
- **b**) Explain the general steps in establishing NP-completeness proof of a given problem.
- c) Write the randomized version of Quick sort algorithm.
- **d)** State the circuit satisfiability problem. Prove the circuit satisfiability problem belongs to the class NP.
- e) Prove that Single and Multi-tape Turning Machines are equivalent.
- **f**) State Godel's incompleteness theorem. Also give one example.
- g) State Rice theorem and its application in domain of complexity.
- h) Write the steps of randomized version of quick sort algorithm with its complexity

SECTION-C

Attempt any two of the following:

 $(15 \times 2 = 30)$

- 3 Explain the following class of problems:
 - i) BPP
 - ii) RP
 - iii) CORP
- 4 Prove that:
 - i) if A is a problem in P, then the complement \bar{A} of A is also in P.
 - ii) if the complement of an NP-complete problem is in NP, then NP = CO NP.
- 5 Write short notes on the following:
 - i) Quantum Computation
 - ii) Communication complexity
 - iii) Parallel Computation