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**B.TECH**  
**(SEM VI) THEORY EXAMINATION 2017-18**  
**DIGITAL CONTROL SYSTEM**

Time: 3 Hours

Total Marks: 100

**Note: 1.** Attempt all Sections. If require any missing data; then choose suitably.

**SECTION A**

**1. Attempt all questions in brief.**

**2 x 10 = 20**

- a) Explain acquisition time for sample and hold operation.
- b) If  $X(z) = 2 + 3Z^{-1} + 4Z^{-2}$  then find the initial and final value of the corresponding sequence.
- c) What are advantages of a control system designing with a high gain feedback?
- d) What do you by insensitive controllers?
- e) Explain the concepts of observability.
- f) What do you mean by the state of digital processor?
- g) What are the uses of Lyapunov stability in adaptive control system?
- h) What do mean by the stability in sense of Lyapunov?
- i) Explain the principle of optimality.
- j) What do you mean by dynamic programming?

**SECTION B**

**2. Attempt any three of the following:**

**10 x 3 = 30**

- a) Derive the transfer function of the following data hold circuit.
  - i. Zero order hold circuit.
  - ii. First order hold circuit.
- b) Explain general structure of a digital structure of a control system.
- c) Discuss some merits and demerits if representing state model into
  - i. Physical variable form
  - ii. Phase variable form
  - iii. Conical variable form
- d) Explain Jury stability criterion. Also list the difference between the Jury stability test and stability analysis using bilinear transformation coupled with Routh stability criterion.
- e) Derive an expression for the discrete Euler-Lagrange equation.

## SECTION C

**3. Attempt any one part of the following: 10 x 1 = 10**

a) Obtain the Z-transform of the following:

(i)  $X(S) = \frac{a}{s^2(s+a)}$  (ii)  $X(S) = \frac{s}{(s^2 - \alpha s^2)}$

b) What do you understand by z-transform? Explain the relationship between the Laplace transform and the Z-transform. Define the constant-Damping Loci.

**4. Attempt any one part of the following: 10 x 1 = 10**

a) What do you mean by transient accuracy of a non unity feedback discrete time system?

b) Explain the designing of a digital compensator using Root Locus.

**5. Attempt any one part of the following: 10 x 1 = 10**

a) A system is described by-

$$\dot{x} = \begin{bmatrix} -1 & -4 & -1 \\ -1 & -6 & -2 \\ -1 & -2 & -3 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} u$$

$$y = [1 \quad 1 \quad 1]x$$

Find the transfer function and construct the signal flow graph.

b) Construct the state model for the system characterized by the differential equation-

$$\frac{d^3 y}{dt^3} + \frac{6d^2 y}{dt^2} + \frac{11dy}{dt} + 6y = u$$

Give the block diagram representation of the state model.

**6. Attempt any one part of the following: 10 x 1 = 10**

a) Consider the discrete time unity feedback control system (T=1 sec) whose open loop pulse transfer function is given by

$$G(z) = \frac{K(0.3679Z + 0.2642)}{(Z - 0.3679)(Z - 1)}$$

Determine the range of K for stability by use of the Jury stability test.

b) Explain in detail the second method of the Liapunov.

**7. Attempt any one part of the following: 10 x 1 = 10**

a) Explain and derive an expression for the discrete maximum or minimum principle.

b) Explain the time-optimal control with energy constraint in detail.