



(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 214219

Roll No.

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MCA

(SEM. II) THEORY EXAM. 2014-15
COMPUTER BASED NUMERICAL
AND STATISTICAL TECHNIQUES

Time : 3 Hours]

[Total Marks : 100

Note : Attempt the questions as indicated.

Q1. Attempt any *four* parts of the following : 5x4=20

(a) Define absolute, relative and percentage error. If 0.333 is the approximate value of $1/3$, find absolute, relative and percentage errors.

(b) Perform the following operations—

i) $.4546 E 3 + .5454 E 8$

ii) $.9432 E - 4 - .6353 E - 6$

- (c) Write a C program to implement Bisection method.
- (d) Find the real root of the equation $x^2 - 5x + 2 = 0$ by Newton-Raphson method.
- (e) Apply false position method to find smallest positive root of the equation $x - e^x = 0$ correct to two decimal places.
- (f) Explain underflow and overflow conditions of error in floating point's addition and subtraction.

Q2. Attempt any *four* parts of the following : $5 \times 4 = 20$

- (a) Solve the following systems of equations by Gauss elimination method—

$$x - y + z = 1$$

$$-3x + 2y - 3z = -6$$

$$2x - 5y + 4z = 5$$

- (b) Apply Gauss's forward formula to find the value of $f(x)$ at $x=3.75$ from the table —

| x | 2.5 | 3.0 | 3.5 | 4.0 | 4.5 | 5.0 |
|------|--------|--------|--------|--------|--------|--------|
| f(x) | 24.145 | 22.043 | 20.225 | 18.644 | 17.262 | 16.047 |

- (c) Given $y_{20}=24$, $y_{24}=32$, $y_{28}=35$ and $y_{32}=40$, find y_{25} by Bessel's interpolation formula.
- (d) Write algorithm for Newton's forward and Newton's backward formula.
- (e) Use Stirling's formula to find y_{28} , given $y_{20}=49225$, $y_{25}=48316$, $y_{30}=47236$, $y_{35}=45926$ and $y_{40}=44306$.
- (f) What do you understand by rate of convergence of a method to find out the root of an equation? Explain.

Q3. Attempt any *two* parts of the following : 10x2=20

- (a) (i) Evaluate $\int_0^6 \frac{dx}{1+x^2}$ by Simpson's 1/3 rule.

- (ii) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ by using Simpson's 3/8 rule.

- (b) Derive Euler-Maclurin formula and use it to prove that –

$$\sum_1^n \chi^2 = \frac{n(n+1)(2n+1)}{6}$$

- (c) Apply Hermite's formula to find a polynomial from the following data –

| | | | |
|-------|---|---|---|
| x | 0 | 1 | 2 |
| f(x) | 0 | 1 | 0 |
| f'(x) | 0 | 0 | 0 |

Q4. Attempt any *two* parts of the following : 10x2=20

- (a) (i) Use the method of least squares to fit the curve–

$$y = \frac{c_0}{x} + c_1 \sqrt{x}$$

- (ii) Find the least square line for the data points–

(-1,10), (0,9), (1,7), (2,5), (3,4), (4,3), (5,0) and (6,-1)

- (b) Obtain y(1.5) from the following data using cubic spline–

x : 1 2 3

y : -8 -1 18

(c) Given the following data—

| | | | | | | | | |
|-----|---|---|---|---|---|---|---|---|
| x | 1 | 5 | 3 | 2 | 1 | 1 | 7 | 3 |
| y | 6 | 1 | 0 | 0 | 1 | 2 | 1 | 5 |

(i) Fit a regression line of y on x .

(ii) Fit a regression line of x on y .

Q5. Attempt any *two* parts of the following : $10 \times 2 = 20$

(a) What is Chi-square test?

A die is thrown 90 times with the following results—

Face : 1 2 3 4 5 6 Total

Frequency : 10 12 16 14 18 20 90

- (b) Find the trend of annual sales of trading organization
moving average method

| | | | | | | | | | | |
|-----------------------------|------|------|------|------|------|------|------|------|------|------|
| Year | 1964 | 1965 | 1966 | 1967 | 1968 | 1969 | 1970 | 1971 | 1972 | 1973 |
| Annual sales Rs. In 1000 | 80 | 84 | 80 | 88 | 98 | 92 | 84 | 88 | 80 | 100 |
| Year | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | 1982 | 1983 |
| Annual sales Rs. In 1000 | 84 | 96 | 92 | 104 | 116 | 112 | 102 | 114 | 108 | 126 |

- (c) Write short notes on the following—

(i) Multiple regression

(ii) Histogram
